

Name

Class



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# Pythagoras theorem

(9 – 1) Topic booklet

## Higher

These questions have been collated from previous years GCSE Mathematics papers.

**You must have:** Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Total Marks

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must **show all your working out.**
- If the question is a **1H** question you are not allowed to use a calculator.
- If the question is a **2H** or a **3H** question, you may use a calculator to help you answer.

### Information

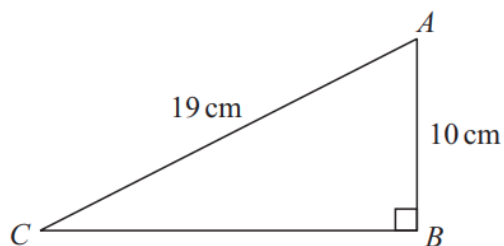
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

**Answer ALL questions**  
**Write your answers in the space provided.**  
**You must write down all the stages in your working.**

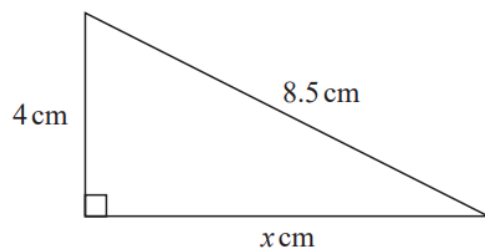
- 1**  $ABC$  is a right-angled triangle.



Work out the length of  $CB$ .  
Give your answer correct to 3 significant figures.

..... cm

1 Here is a right-angled triangle.



Work out the value of  $x$ .

$x =$  .....

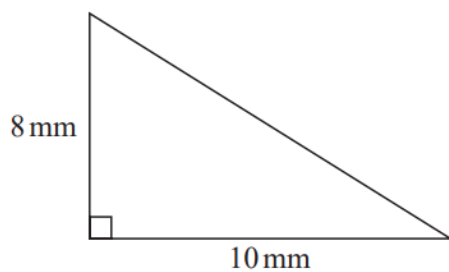
**4** Triangle  $ABC$  has perimeter 20 cm.

$$AB = 7 \text{ cm.}$$

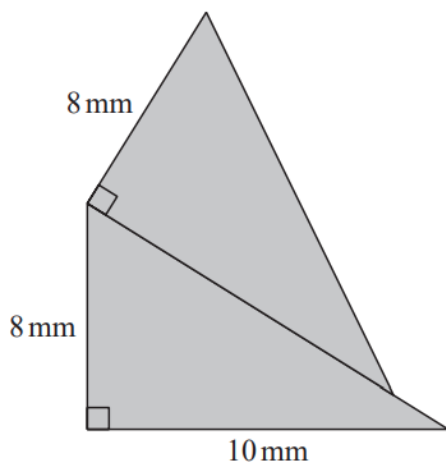
$$BC = 4 \text{ cm.}$$

By calculation, deduce whether triangle  $ABC$  is a right-angled triangle.

5 Here is a right-angled triangle.



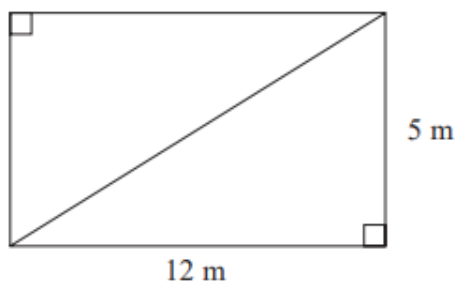
The shaded shape below is made from two of these triangles.



Work out the perimeter of the shaded shape.  
Give your answer correct to 3 significant figures.

..... mm

- 5 This rectangular frame is made from 5 straight pieces of metal.

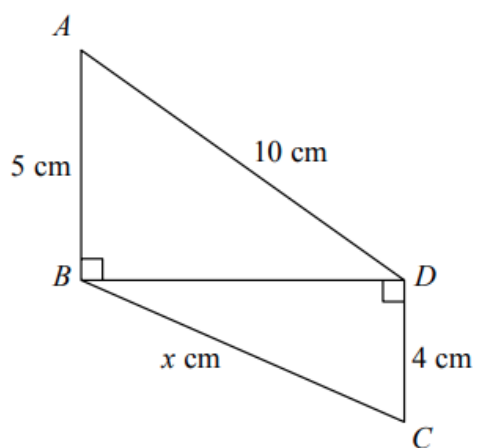


The weight of the metal is 1.5 kg per metre.

Work out the total weight of the metal in the frame.

..... kg

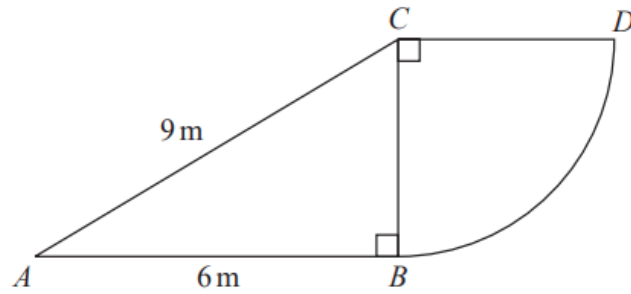
6 Triangles  $ABD$  and  $BCD$  are right-angled triangles.



Work out the value of  $x$ .

Give your answer correct to 2 decimal places.

- 7 The diagram shows a right-angled triangle and a quarter circle.

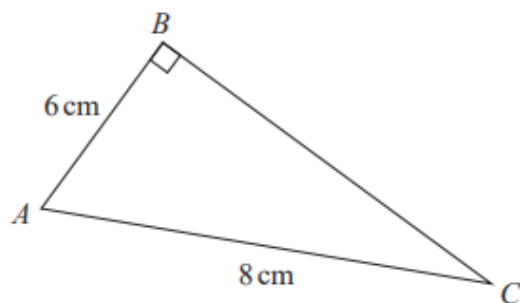


The right-angled triangle  $ABC$  has angle  $ABC = 90^\circ$   
The quarter circle has centre  $C$  and radius  $CB$ .

Work out the area of the quarter circle.  
Give your answer correct to 3 significant figures.  
You must show all your working.

.....  $\text{m}^2$

8  $ABC$  is a right-angled triangle.



Here is Sarah's method to find the length of  $BC$ .

$$\begin{aligned}BC^2 &= AB^2 + AC^2 \\&= 6^2 + 8^2 \\&= 100 \\BC &= 10\end{aligned}$$

What mistake has Sarah made in her method?

.....

.....

.....

(1)

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**(Total for Question 8 is 1 mark)**

- 8** A square, with sides of length  $x$  cm, is inside a circle.  
Each vertex of the square is on the circumference of the circle.

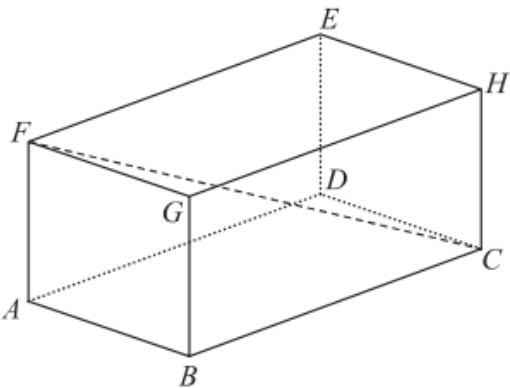


The area of the circle is  $49 \text{ cm}^2$ .

Work out the value of  $x$ .

Give your answer correct to 3 significant figures.

12 The diagram shows a cuboid  $ABCDEFGH$ .

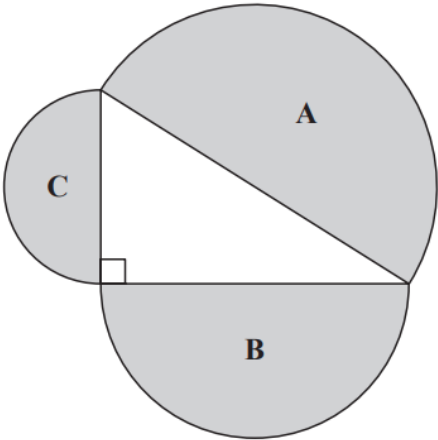


$AB = 7\text{ cm}$ ,  $AF = 5\text{ cm}$  and  $FC = 15\text{ cm}$ .

Calculate the volume of the cuboid.  
Give your answer correct to 3 significant figures.

.....  $\text{cm}^3$

**13** A right-angled triangle is formed by the diameters of three semicircular regions, **A**, **B** and **C** as shown in the diagram.



Show that

$$\text{area of region A} = \text{area of region B} + \text{area of region C}$$

**13**  $A$  and  $B$  are points on a centimetre grid.

$A$  is the point with coordinates  $(-7, 6)$

$B$  is the point with coordinates  $(8, -5)$

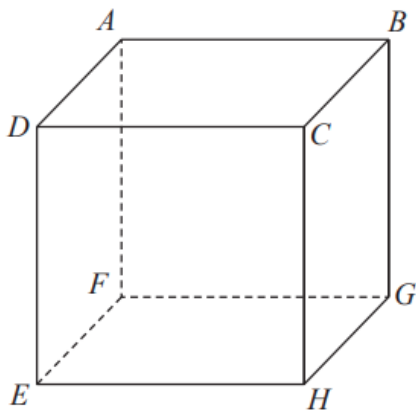


Work out the length of  $AB$ .

Give your answer correct to 1 decimal place.

..... cm

18 The diagram shows a cube.

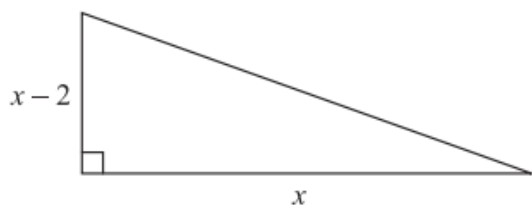


$AH = 11.3$  cm correct to the nearest mm.

Calculate the lower bound for the length of an edge of the cube.  
You must show all your working.

..... cm

19 Here is a right-angled triangle.



All measurements are in centimetres.

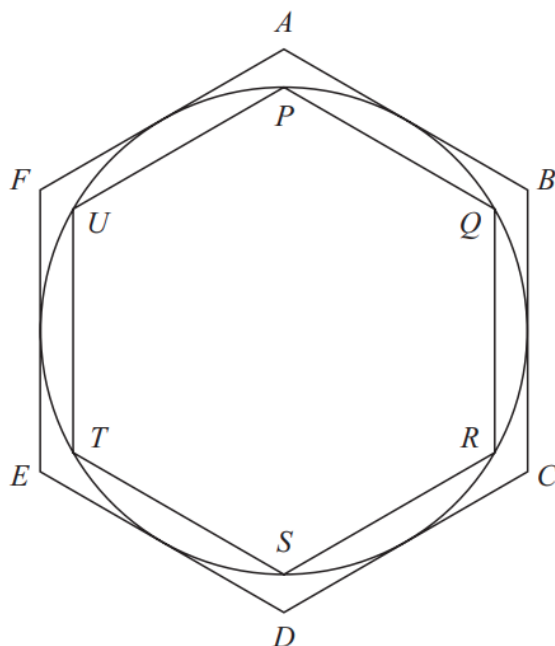
The area of the triangle is  $2.5 \text{ cm}^2$ .

Find the perimeter of the triangle.

Give your answer correct to 3 significant figures.

You must show all of your working.

21 The diagram shows a circle, radius  $r$  cm and two regular hexagons.

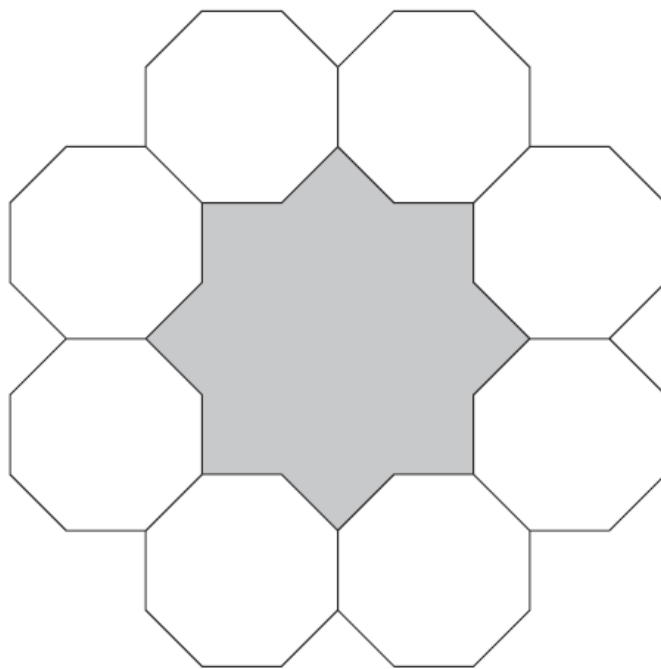


Each side of the larger hexagon  $ABCDEF$  is a tangent to the circle.  
Each side of the smaller hexagon  $PQRSTU$  is a chord of the circle.

By considering perimeters, show that

$$3 < \pi < 2\sqrt{3}$$

24 The diagram shows 8 identical regular octagons joined to enclose a shaded shape.



Each octagon has sides of length  $a$ .

Find, in terms of  $a$ , an expression for the area of the shaded shape.

Give your answer in the form  $p(2 + \sqrt{2})a^2$  where  $p$  is an integer.

You must show all your working.